

Problem #1

a.) $(f+g)(x) = f(x)+g(x)$
 $= (3x^2-4x+2) + (-4x^2+2x+8)$
 $= -x^2-2x+10$

b.) $(f-h)(x) = f(x)-h(x)$

$$\begin{aligned} &= (6-1-4) \\ &= 10 \end{aligned}$$

$$\begin{aligned} f(x) &= 3(x)^2-4(x)+2 \\ &= 3 \cdot 4 - 4 \cdot 2 + 2 \\ &= 12 - 8 + 2 = 6 \end{aligned}$$

$$\begin{aligned} h(x) &= -4(x)^2+2(x)+8 \\ &= -16 + 4 + 8 \\ &= -4 \end{aligned}$$

c.) $(\frac{f}{h})(x) = \frac{f(x)}{h(x)} = \frac{3x^2-4x+2}{-4x^2+2x+8}$

d.) $f(x-3) = 3(x-3)^2-4(x-3)+2 = 3(x^2-6x+9)-4x+12+2$
 $= 3x^2-18x+27-4x+12$
 $= 3x^2-22x+39$

e.) $(g \circ h)(x) = g(h(x)) = g(-4x^2+2x+8) = \frac{5(-4x^2+2x+8)}{(-4x^2+2x+8)-4} = \frac{-20x^2+10x+40}{-4x^2+2x+4}$

f.) $(h \circ f)(x) = h(f(x)) = h(3x^2-4x+2) = -4(3x^2-4x+2)^2+2(3x^2-4x+2)+8$
 $= -4(9x^4-24x^3+28x^2-16x+4) + 2(3x^2-4x+2)+8$
 $= -36x^4+96x^3-112x^2+64x-16+6x^2-8x+4+8$
 $= -36x^4+96x^3-106x^2+56x-4$

g.) Domain $(f+g) = \{x | x \neq 4\}$

h.) Domain $(h \cdot k) = \{x | x \neq -5\}$

i.) Domain $(\frac{f}{k}) = \{x | x \neq 4, -5, 3\}$

$$\begin{aligned} k(x) &= \frac{x-3}{x+5} = 0 \\ x-3 &= 0 \\ x &= 3 \end{aligned}$$

j.) Domain $(g \circ k) = \{x | x \neq -5, -23/5\}$



$$\begin{aligned} \frac{x-3}{x+5} &= 4 \\ x-3 &= 4x+20 \\ -23 &= 5x \end{aligned}$$

Problem #2

a.) $f(x) = x^2 - 6x + 9$

vertex: $x = -\frac{b}{2a} = \frac{-(-6)}{2(1)} = 3$

$$f(3) = (3)^2 - 6(3) + 9 \\ = 9 - 18 + 9 = 0$$

(3, 0)

axis of symmetry: $x = 3$

x-intercept(s): $x^2 - 6x + 9 = 0$

$(x-3)^2 = 0$

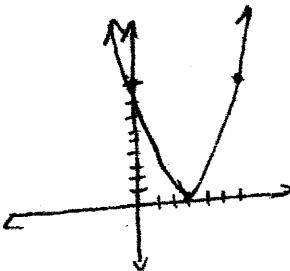
(3, 0)

$x-3 = 0$

$x = 3$

y-intercept: $y = 0^2 - 6(0) + 9 = 9$

(0, 9)



symmetric point (6, 9)

b.) $f(x) = 2x^2 - x + 2$

vertex: $x = -\frac{b}{2a} = \frac{-(-1)}{2(2)} = \frac{1}{4}$

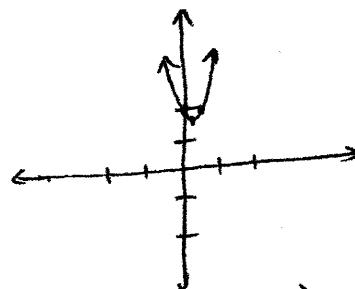
$$f(\frac{1}{4}) = 2(\frac{1}{4})^2 - \frac{1}{4} + 2 \\ = \frac{1}{8} - \frac{1}{4} + 2 = \frac{1-2+16}{8} = \frac{15}{8} \\ (\frac{1}{4}, \frac{15}{8})$$

axis of symmetry: $x = \frac{1}{4}$

x-intercept(s): $2x^2 - x + 2 = 0$

$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(2)(2)}}{2(2)} \\ = \frac{1 \pm \sqrt{1-16}}{4} = \frac{1 \pm \sqrt{-15}}{4} \\ = \frac{1 \pm i\sqrt{15}}{4} \leftarrow \text{No x-intercepts.}$$

y-intercept: $y = 2(0)^2 - (0) + 2 = 2 \\ (0, 2)$

symmetric point ($\frac{1}{4}, \frac{15}{8}$)

c.) $f(x) = 2x^2 + 5x + 3$

vertex: $x = -\frac{b}{2a} = -\frac{5}{2(2)} = -\frac{5}{4}$

$$f(-\frac{5}{4}) = 2(-\frac{5}{4})^2 + 5(-\frac{5}{4}) + 3 \\ = \frac{25}{8} - \frac{25}{4} + 3 = \frac{25-50+24}{8} = -\frac{1}{8} \\ (-\frac{5}{4}, -\frac{1}{8})$$

axis of symmetry: $x = -\frac{5}{4}$

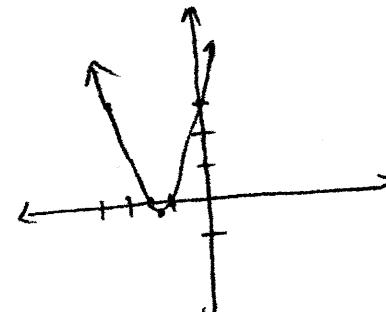
x-intercept(s): $2x^2 + 5x + 3 = 0$

$(2x+3)(x+1) = 0$

$x = -\frac{3}{2}, x = -1$

(- $\frac{3}{2}$, 0) (-1, 0)

y-intercept: $y = 2(0)^2 + 5(0) + 3 \\ (0, 3)$

symmetric point: $(-\frac{5}{4}, \frac{1}{8})$ Problem #3

a.) zeros: -4, 3, 5 degree: 3

$y = (x+4)(x-3)(x-5)$

$y = (x^2+x-12)(x-5)$

$y = x^3 - 5x^2 + x^2 - 5x - 12x + 60$

$y = x^3 - 4x^2 - 17x + 60$

b.) zeros: -3, -1, 2, 5 degree: 4

$y = (x+3)(x+1)(x-2)(x-5)$

$y = (x^2+4x+3)(x^2-7x+10)$

$y = x^4 - 7x^3 + 10x^2 + 4x^3 - 2x^2 + 40x + 3x^2 - 21x + 30$

$y = x^4 - 3x^3 - 15x^2 + 19x + 30$

c.) zeros: 3, 4-i degree: 3

$y = (x-3)(x-(4-i))(x-(4+i))$

$y = (x-3)(x-4+i)(x-4-i)$

$y = (x-3)(x^2 - 4x - ix - 4x + 16 + 4i + ix - 4i - i^2)$

$y = (x-3)(x^2 - 8x + 17)$

$y = x^3 - 8x^2 + 17x - 3x^2 + 24x - 51$

$y = x^3 - 11x^2 + 41x - 51$

d.) zeros: 1, 2, 2+i degree: 4

$y = (x-1)(x-2)(x-(2+i))(x-(2-i))$

$y = (x^2 - 3x + 2)(x-2-i)(x-2+i)$

$y = (x^2 - 3x + 2)(x^2 - 2x + ix - 2x + 4 - 2i - ix + 2i - i^2)$

$y = (x^2 - 3x + 2)x^2 - 4x + 5$

$y = x^4 - 4x^3 + 5x^2 - 3x^3 + 12x^2 - 15x + 2x^2 - 8x + 10$

$y = x^4 - 7x^3 + 19x^2 - 23x + 10$

MATH 130 EXAM #2 REVIEW KEY - SPRING 2013

Problem #4

a.) $f(x) = x^3 + 2x^2 - 3x + 1$ $g(x) = x + 1$

$$\begin{array}{r} -1 \sqrt{1 \ 2 \ -3 \ 1} \\ \underline{-1 \ -1 \ 4} \\ 1 \ 1 \ -4 \ 1 \end{array}$$

$$G(x) = x^2 + x - 4 \quad R = 5$$

b.) $f(x) = -4x^3 + 2x^2 - x + 1$ $g(x) = x + 3$

$$\begin{array}{r} -2 \sqrt{-4 \ 2 \ -1 \ 1} \\ \underline{-8 \ -20 \ 40} \\ -4 \ 10 \ -21 \ 1 \end{array}$$

$$G(x) = -4x^2 + 10x - 21 \quad R = 43$$

c.) $f(x) = x^4 + x^3 + 2$ $g(x) = x - 2$

$$\begin{array}{r} 2 \sqrt{1 \ 0 \ 1 \ 0 \ 2} \\ \underline{2 \ 4 \ 10 \ 20} \\ 1 \ 3 \ 5 \ 10 \ 12 \end{array}$$

$$G(x) = x^3 + 2x^2 + 5x + 10 \quad R = 28$$

d.) $f(x) = x^5 + 1$ $g(x) = x + 1$

$$\begin{array}{r} -1 \sqrt{1 \ 0 \ 0 \ 0 \ 0 \ 1} \\ \underline{-1 \ 1 \ -1 \ 1 \ -1} \\ 1 \ -1 \ -1 \ 1 \ 0 \end{array}$$

$$G(x) = x^4 - x^3 + x^2 - x + 1 \quad R = 0$$

Problem #5

a.) $f(x) = -4x^3 + 5x^2 + 8$; $x + 3$

$$\begin{array}{r} -3 \sqrt{-4 \ 5 \ 0 \ 8} \\ \underline{-12 \ -15 \ 15 \ 3} \\ -4 \ 17 \ -51 \ 16 \end{array}$$

Not a factor

b.) $f(x) = 2x^6 - 18x^4 + x^2 - 9$; $x + 3$

$$\begin{array}{r} -3 \sqrt{2 \ 0 \ -18 \ 0 \ 1 \ 0 \ -9} \\ \underline{-6 \ 18 \ 0 \ 0 \ -3 \ 9} \\ 2 \ -6 \ 0 \ 0 \ 1 \ -3 \ 10 \end{array}$$

Is a factor

c.) $f(x) = 4x^4 - 15x^2 - 4$; $x - 2$

$$\begin{array}{r} 2 \sqrt{4 \ 0 \ -15 \ 0 \ -4} \\ \underline{8 \ 16 \ 2 \ 4} \\ 4 \ 8 \ 1 \ 2 \ 10 \end{array}$$

Is a factor

Problem #6

b.) $x^4 - 5x^3 + 3x^2 + 15x - 18 = 0$

$$P: \pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$$

$$Q: \pm 1$$

$$P/Q: \pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$$

$$\begin{array}{r} 2 \sqrt{1 \ -5 \ 3 \ 15 \ -18} \\ \underline{2 \ -6 \ -6 \ 18} \\ 1 \ -3 \ -3 \ 9 \ 10 \end{array}$$

$$(x-2)(x^3 - 3x^2 - 3x + 9)$$

$$(x-2)(x-3)(x^2 - 3) = 0$$

$$x-2=0$$

$$x=2$$

$$x-3=0$$

$$x=3$$

$$x^2 - 3 = 0$$

$$x^2 = 3$$

$$\begin{array}{r} 3 \sqrt{1 \ -3 \ -3 \ 9} \\ \underline{3 \ 0 \ -9} \\ 1 \ 0 \ -3 \ 10 \end{array}$$

c.) $2x^3 + 3x^2 + 2x + 3 = 0$

$$P: \pm 1, \pm 3$$

$$Q: \pm 1, \pm 2$$

$$P/Q: \pm 1, \pm 3, \pm \frac{1}{2}, \pm \frac{3}{2}$$

$$\begin{array}{r} -3 \sqrt{2 \ 3 \ 2 \ 3} \\ \underline{-3 \ 0 \ -3} \\ 2 \ 0 \ 2 \ 10 \end{array}$$

$$(x + \frac{3}{2})(2x^2 + 2) = 0$$

$$x + \frac{3}{2} = 0 \quad 2x^2 + 2 = 0$$

$$x = -\frac{3}{2} \quad x^2 = -1$$

$$x = \pm i$$

$$x = -\frac{3}{2}, \pm i$$

d.) $2x^3 - 11x^2 + 10x + 8 = 0$

$$P: \pm 1, \pm 2, \pm 4, \pm 8$$

$$Q: \pm 1, \pm 2$$

$$P/Q: \pm 1, \pm 2, \pm 4, \pm 8, \pm \frac{1}{2}$$

$$\begin{array}{r} 2 \sqrt{2 \ -11 \ 10 \ 8} \\ \underline{4 \ -14 \ -8} \\ 2 \ -7 \ -4 \ 10 \end{array}$$

$$(x-2)(2x^2 - 7x - 4) = 0$$

$$(x-2)(2x+1)(x-4) = 0$$

$$x = 2, -\frac{1}{2}, 4$$

Problem #6 continued

a.) $3x^3 - 5x^2 + 2x - 8 = 0$

$P: \pm 1, \pm 2, \pm 4, \pm 8$

$Q: \pm 1, \pm 3$

$\frac{P}{Q}: \pm 1, \pm 2, \pm 4, \pm 8, \pm \frac{1}{3}, \pm \frac{2}{3}, \pm \frac{4}{3}, \pm \frac{8}{3}$

$$\begin{array}{r} \overline{3 - 5 2 - 8} \\ 6 8 \\ \hline 3 1 4 10 \end{array}$$

$x - 2 = 0$

$\boxed{x = 2}$

$3x^2 + x + 4 = 0$

$x = \frac{-1 \pm \sqrt{1^2 - 4(3)(4)}}{2(3)}$

$$\boxed{x = \frac{-1 \pm i\sqrt{47}}{6}}$$

$(x-2)(3x^2 + x + 4) = 0$

f.) $x^3 - 8x^2 + 25x - 26 = 0$

$P: \pm 1, \pm 2, \pm 13, \pm 26$

$Q: \pm 1$

$\frac{P}{Q}: \pm 1, \pm 2, \pm 13, \pm 26$

$$\begin{array}{r} \overline{251 - 8 25 - 26} \\ 2 -10 26 \\ \hline 1 -6 13 10 \end{array}$$

$(x-2)(x^2 - 6x + 13) = 0$

$x - 2 = 0 \quad x^2 - 6x + 13 = 0$

$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(13)}}{2(1)}$

$x = \frac{6 \pm 4i}{2} = \frac{6}{2} \pm \frac{4i}{2}$

$$\boxed{x = 2 \quad x = 3 \pm 2i}$$

e.) $x^4 - 2x^3 + 10x^2 - 18x + 9 = 0$

$P: \pm 1, \pm 3, \pm 9$

$Q: \pm 1$

$\frac{P}{Q}: \pm 1, \pm 3, \pm 9$

$$\begin{array}{r} \overline{1 - 2 10 - 18 9} \\ 1 -1 9 -9 \\ \hline 1 -1 9 -9 0 \end{array}$$

$(x-1)(x^3 - x^2 + 9x - 9)$

$$\begin{array}{r} \overline{1 - 1 9 - 9} \\ 1 0 9 \\ \hline 1 0 9 0 \end{array}$$

$(x-1)(x-1)(x^2 + 9) = 0$

$x-1=0 \quad x-1=0 \quad x^2+9=0$

$$\boxed{x = 1, \pm 3i}$$

g.) $2x^4 + x^3 - 35x^2 - 113x + 65 = 0$

$P: \pm 1, \pm 5, \pm 13, \pm 65$

$Q: \pm 1, \pm 2$

$\frac{P}{Q}: \pm 1, \pm 5, \pm 13, \pm 65, \pm \frac{1}{2}, \pm \frac{5}{2}, \pm \frac{13}{2}, \pm \frac{65}{2}$

$$\begin{array}{r} \overline{2 1 - 35 - 113 65} \\ 1 1 -17 + 65 \\ \hline 2 2 -34 - 130 0 \end{array}$$

$(x-16)(2x^3 + 2x^2 - 34x - 130) = 0$

$2(x-\frac{1}{2})(x^3 + x^2 - 17x - 65) = 0$

$$\begin{array}{r} \overline{551 1 - 17 - 65} \\ 5 30 65 \\ \hline 1 6 13 0 \end{array}$$

$2(x-\frac{1}{2})(x-5)(x^2 + 6x + 13) = 0$

$$\boxed{x = \frac{1}{2}, 5, 3 \pm 2i}$$

Problem #7

a) $f(x) = x^3 - 2x^2 - 9x + 18$
 $= (x^3 - 2x^2) - (9x - 18)$
 $= x^2(x - 2) - 9(x - 2)$
 $= (x - 2)(x^2 - 9)$
 $f(x) = (x - 2)(x + 3)(x - 3)$

x-int: $(x - 2)(x + 3)(x - 3) = 0$
 $(2, 0) (-3, 0) (3, 0)$

y-int: $y = (0 - 2)(0 + 3)(0 - 3)$
 $y = (-2)(3)(-3) = 18$
 $(0, 18)$

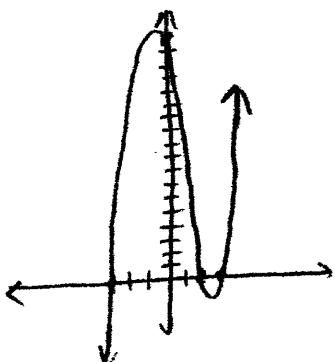
End behavior: $y = x^3 \rightarrow \uparrow$

Multiplicities:
 $x = 2$ mult 1 crosses x-axis
 $x = -3$ mult 1 crosses x-axis
 $x = 3$ mult 1 crosses x-axis

Table of Signs:

	-3	2	3
$x - 2$	-	+	+
$x + 3$	+	+	+
$x - 3$	-	-	+
	+	-	+

below above below above
x-axis x-axis x-axis x-axis



b) $f(x) = x^4 - 10x^2 + 9$
 $= (x^2 - 9)(x^2 - 1)$
 $f(x) = (x + 3)(x - 3)(x + 1)(x - 1)$

x-int: $(x + 3)(x - 3)(x + 1)(x - 1) = 0$
 $(-3, 0) (3, 0) (-1, 0) (1, 0)$

y-int: $y = (0 + 3)(0 - 3)(0 + 1)(0 - 1)$
 $= (3)(-3)(1)(-1) = 9$
 $(0, 9)$

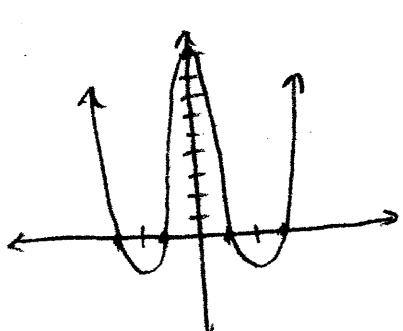
End behavior: $y = x^4 \rightarrow \uparrow \uparrow$

Multiplicities:
 $x = 3$ mult 1 crosses x-axis
 $x = -3$ mult 1 crosses x-axis
 $x = 1$ mult 1 crosses x-axis
 $x = -1$ mult 1 touches x-axis

Table of Signs

	-3	-1	1	3
$x + 3$	-	+	+	+
$x - 3$	+	-	-	+
$x + 1$	-	+	+	+
$x - 1$	+	-	+	+
	+	-	+	+

above below above below above
x-axis x-axis x-axis x-axis x-axis



c) $f(x) = -3(x - 7)(x + 3)^2$
 $x = 7: -3(x - 7)(x + 3)^2 = 0$
 $-3 = 0 \quad x - 7 = 0 \quad (x + 3)^2 = 0$
 $x \quad x = 7 \quad x = -3$
 $(7, 0) \quad (-3, 0)$

y-int: $y = -3(0 - 7)(0 + 3)^2$
 $y = (-3)(-7)(9) = 189$
 $(0, 189)$

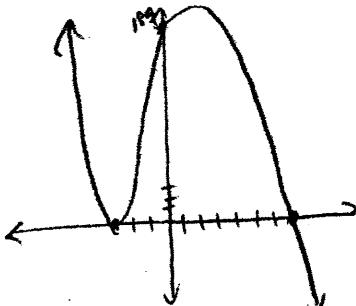
End behavior: $y = -3x^3 \rightarrow \downarrow$

Multiplicities:
 $x = 7$ mult 1 crosses x-axis
 $x = -3$ mult 2 touches x-axis

Table of Signs

	-3	7
-3	-	-
$x - 7$	-	-
$(x + 3)^2$	+	+
	+	-

above below above below below
x-axis x-axis x-axis x-axis x-axis



Problem #7 continued

d.) $f(x) = (x-\frac{1}{3})^2(x-1)^3 = 0$

x-int: $(x-\frac{1}{3})^2(x-1)^3 = 0$

$(x-\frac{1}{3})^2 = 0 \quad (x-1)^3 = 0$

$x = \frac{1}{3} \quad x = 1$

$(\frac{1}{3}, 0) \quad (1, 0)$

y-int: $y = (0-\frac{1}{3})^2(0-1)^3$

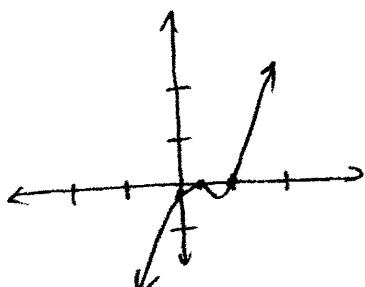
$y = (\frac{1}{3})(-1) = -\frac{1}{3}$

$(0, -\frac{1}{3})$

End Behavior: $y = x^5 \uparrow \uparrow$ multiplicities: $x = \frac{1}{3}$ mult 2 touches x-axis
 $x = 1$ mult 3 crosses x-axis

Table of Signs:

	$\frac{1}{3}$	1
$(x-\frac{1}{3})^2$	+	+
$(x-1)^3$	-	+
	-	+
below x-axis	below x-axis	above x-axis



e.) $f(x) = x^2(x-3)(x+1)$

x-int: $x^2(x-3)(x+1) = 0$

$x^2 = 0 \quad x-3 = 0 \quad x+1 = 0$

$x = 0 \quad x = 3 \quad x = -1$

$(0, 0) \quad (3, 0) \quad (-1, 0)$

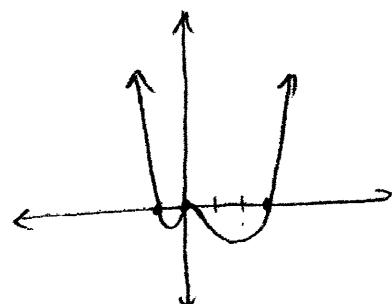
y-int: $y = (0)^2(0-3)(0+1)$

$y = 0 \quad (0, 0)$

End Behavior: $y = x^4 \uparrow \uparrow$ multiplicities: $x=0$ mult 2 touches x-axis
 $x=3$ mult 1 crosses x-axis
 $x=-1$ mult 1 crosses x-axis

Table of Signs

	-1	0	3
x^2	+	+	+
$x-3$	-	-	+
$x+1$	-	+	+
	+	-	+
above x-axis	below x-axis	below x-axis	above x-axis

Problem #8

a.) $f(x) = \frac{3x-2}{x^2-4x+3} = \frac{3x-2}{(x-3)(x-1)}$

x-int: $3x-2 = 0 \quad x = \frac{2}{3} \quad (\frac{2}{3}, 0)$

y-int: $y = \frac{3(0)-2}{(0-3)(0-1)} = -\frac{2}{3} \quad (0, -\frac{2}{3})$

vertical asymptote(s):

$(x-3)(x-1) = 0$

$x=3, x=1$

horizontal asymptote:

degree numerator = 1
degree denominator = 2 $y=0$

holes: none

check if graph intersects horizontal asymptote:

$\frac{3x-2}{(x-3)(x-1)} = 0$

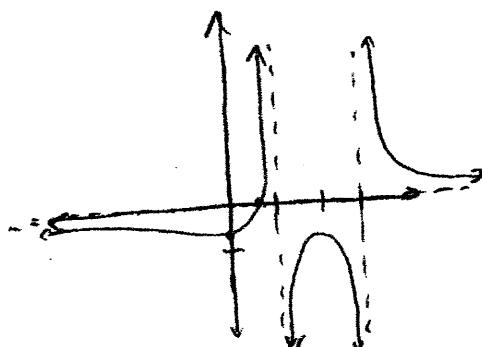
$3x-2 = 0$

$x = \frac{2}{3}$

Intersects at $x = \frac{2}{3}$

Table of Signs

	$\frac{2}{3}$	1	3
$3x-2$	-	+	+
$x-3$	-	-	+
$x-1$	-	-	+
	+	-	+
below x-axis	above x-axis	below x-axis	above x-axis



Problem #8 continued

b) $f(x) = \frac{3x-4}{x-3}$

x-int: $3x-4=0$
 $x=\frac{4}{3} \quad (4/3, 0)$

y-int: $y = \frac{3(0)-4}{0-3} = \frac{-4}{3} \quad (0, -4/3)$

vertical asymptote(s):

$$x-3=0 \\ x=3$$

horizontal asymptote

$$\text{degree numerator} = 1 \\ \text{degree denominator} = 1 \quad y = \frac{3}{1} \\ y = 3$$

holes: none

check if graph intersects horizontal asymptote:

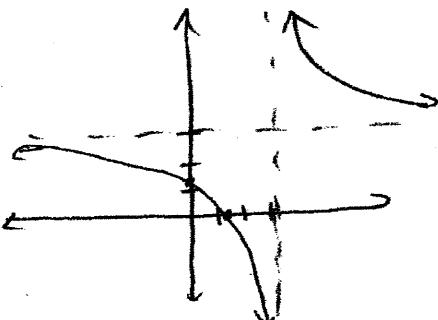
$$\frac{3x-4}{x-3} = 3$$

$$3x-4 = 3x-9 \\ -4 = -9 \quad \text{does not intersect}$$

Table of Signs:

	$\frac{4}{3}$	3
$3x-4$	-	+
$x-3$	-	+
	+	-

above x-axis below x-axis above x-axis



c) $f(x) = \frac{x^2-3x-4}{x+2} = \frac{(x-4)(x+1)}{x+2}$

x-int: $(x-4)(x+1)=0$
 $x=4, -1 \quad (4, 0), (-1, 0)$

y-int: $y = \frac{(0-4)(0+1)}{0+2} = -2 \quad (0, -2)$

vertical asymptote(s):

$$x+2=0 \\ x=-2$$

horizontal/oblique asymptote:

$$\text{degree numerator} = 3 \quad \text{oblique} \\ \text{degree denominator} = 1$$

$$\begin{array}{r} x-5 \\ x+2) x^2-3x-4 \\ - (x^2 + 2x) \\ \hline -5x-4 \\ - (-5x - 10) \\ \hline 6 \end{array}$$

$$y = x-5$$

holes: none

check if graph intersects oblique asymptote:

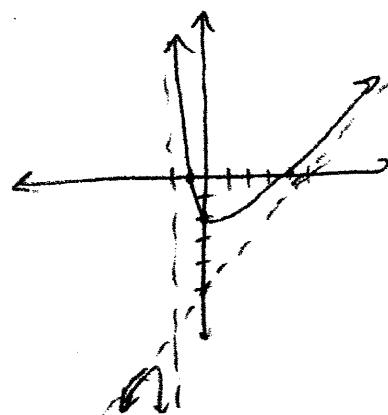
$$\frac{x^2-3x+4}{x+2} = x-5$$

$$x^2-3x+4 = x^2-3x-10 \\ 14 \neq -10 \quad \text{does not intersect}$$

Table of Signs:

	-2	-1	4
$x-4$	-	-	+
$x+1$	-	+	+
$x+2$	+	+	+
	+	-	+

below x-axis above x-axis below x-axis above x-axis

Problem #9

a) $y = \frac{3x+4}{9-5x}$

$$\text{degree numerator} = 1 \\ \text{degree denominator} = 1 \\ y = \frac{3}{-5}$$

b) $y = \frac{4x^2-5x+2}{2x-3}$

$$\text{degree numerator} = 2 \\ \text{degree denominator} = 1 \quad \text{oblique}$$

$$\begin{array}{r} 2x+\frac{1}{2} \\ 2x-3) 4x^2-5x+2 \\ - (4x^2-6x) \\ \hline x+2 \\ - (x-\frac{3}{2}) \\ \hline \frac{7}{2} \end{array}$$

$$y = 2x + \frac{1}{2}$$

Problem #10

a) $y = \frac{3x}{x^2+5x+6}$

$$x^2+5x+6 = 0 \\ (x+2)(x+3) = 0 \\ x = -2, x = -3$$

b) $y = \frac{6x}{x^3-4x^2+4x}$

$$x^3-4x^2+4x = 0 \\ x(x^2-4x+4) = 0 \\ x(x-2)^2 = 0 \\ x = 0, x = 2$$

Problem #11

$$l + \partial w = 400$$

$$A = lw$$

\downarrow max

$$\partial l = 400 - \partial w$$

$$l = 200 - \frac{1}{2}w$$

$$A = (200 - w)w$$

$$A = -w^2 + 200w \leftarrow \curvearrowleft$$

$$w = -\frac{b}{2a}$$

$$w = \frac{-200}{2(-1)} = 100$$

$$l = 200 - 100 = 100$$

$$l = 100 \text{ ft}$$

$$w = 100 \text{ ft}$$

Problem #12



$$l + \partial w = 4000$$

$$A = lw$$

\downarrow max

$$l = 4000 - \partial w$$

$$A = (4000 - \partial w)w$$

$$A = -\partial w^2 + 4000w \leftarrow \curvearrowleft$$

$$w = -\frac{b}{2a}$$

$$w = \frac{-4000}{2(-1)} = 2000$$

$$l = 4000 - 2(2000) = 2000$$

$$l = 2000 \text{ m}$$

$$w = 2000 \text{ m}$$

Problem #13

$$y = kx$$

$$y = 9, x = 30$$

$$y = \frac{3}{10}x$$

$$9 = k \cdot 30$$

$$k = \frac{3}{10}$$

$$y = \frac{3}{10} \cdot 100$$

$$y = 12$$

Problem #14

$$y = \frac{k}{x}$$

$$y = 80, x = 1/4$$

$$80 = \frac{k}{1/4}$$

$$k = 5$$

$$y = \frac{5}{x}$$

$$y = \frac{5}{15}$$

$$y = 1/3$$

Problem #15

$$m = kz^p$$

$$m = 10, z = 2, p = 7.5$$

$$m = \frac{2}{3}z^p$$

$$10 = k(2)(7.5)$$

$$m = \frac{2}{3}(2)(9)$$

$$k = \frac{2}{3}$$

$$m = 36$$

Problem #16

$$P = \frac{kz^2}{r}$$

$$P = \frac{32}{5}, z = 4, r = 10$$

$$P = \frac{4z^2}{r}$$

$$\frac{32}{5} = k(4)^2$$

$$P = \frac{4(3)^2}{32}$$

$$\frac{32}{5} = k \cdot \frac{16}{10}$$

$$P = \frac{9}{8}$$

$$4 = k$$

Problem #17

a.) $f(x) = x^5 + 2$

$y = x^5 + 2$

$x = y^5 + 2$

$x - 2 = y^5$

$\sqrt[5]{x-2} = \sqrt[5]{y^5}$

$y = \sqrt[5]{x-2}$

$f^{-1}(x) = \sqrt[5]{x-2}$

b.) $f(x) = 4x - 3$

$y = 4x - 3$

$x = 4y - 3$

$\frac{x+3}{4} = \frac{4y}{4}$

$y = \frac{x+3}{4}$

$f^{-1}(x) = \frac{x+3}{4}$

c.) $f(x) = \frac{2}{x-3}$

$y = \frac{2}{x-3}$

$x = \frac{2}{y-3}$

$x(y-3) = 2$

$xy - 3x = 2$

$\frac{xy}{x} = \frac{2+3x}{x}$

$y = \frac{2+3x}{x}$

$f^{-1}(x) = \frac{2+3x}{x}$

d.) $f(x) = \frac{f}{x}$

$y = \frac{f}{x}$

$x = \frac{1}{y}$

$xy = 1$

$y = \frac{f}{x}$

$f^{-1}(x) = \frac{f}{x}$

Problem #18 and #19 not on exam #2