

2pts

$$1a \quad 5(-3, 6, 2) - 3(5, 4, 7)$$

$$\langle -15, 30, 10 \rangle + \langle -15, -12, -21 \rangle = \langle -30, 18, -11 \rangle$$

2pts

$$b. \quad \langle -3, 6, 2 \rangle \cdot \langle 5, 4, 7 \rangle = -15 + 24 + 14 = 23$$

3pts

$$c. \quad \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|} \quad \frac{|\vec{b}|}{|\vec{b}|}$$

$$|\vec{b}| = \sqrt{25 + 16 + 49} = \sqrt{90} = 3\sqrt{10}$$

$$\frac{23}{90} \langle -3, 6, 2 \rangle = \left\langle \frac{115}{90}, \frac{92}{90}, \frac{16}{90} \right\rangle$$

4pts

$$d.) \quad \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -3 & 6 & 2 \\ 5 & 4 & 7 \end{vmatrix} = \hat{i}(42 - 8) - \hat{j}(-21 - 10) + \hat{k}(-12 - 30) \\ = 34\hat{i} + 31\hat{j} - 42\hat{k}$$

3pts

$$e.) \quad \sqrt{34^2 + 31^2 + 42^2} = \sqrt{3081}$$

4pts

$$2.) \quad W = \vec{F} \cdot \vec{D} = |\vec{F}| |\vec{D}| \cos \theta \\ = (35 \text{ lb})(85 \text{ ft}) \cos 40^\circ \\ = 2975 \cos 40^\circ = 2279.0 \text{ ft-lb.}$$

3pts

$$3.) \quad P(5, 3, -2) \quad Q(4, -1, 6) \quad \vec{PQ} = \langle -1, -4, 8 \rangle$$

$$x = 5 - t$$

$$y = 3 - 4t$$

$$z = -2 + 8t$$

4pts

$$4.) \quad P(4, -2, 3) \quad Q(3, 5, 1) \quad R(2, 6, -3)$$

$$\vec{PQ} = \langle -1, 7, -2 \rangle$$

$$\vec{PR} = \langle -2, 8, -6 \rangle$$

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -1 & 7 & -2 \\ -2 & 8 & -6 \end{vmatrix} = \hat{i}(-42 + 16) - \hat{j}(6 - 4) + \hat{k}(-8 + 14) \\ = -26\hat{i} - 2\hat{j} + 6\hat{k}$$

$$-26(x - 4) - 2(y + 2) + 6(z - 3) = 0$$

$$-26x + 104 - 2y - 4 + 6z - 18 = 0$$

$$-26x - 2y + 6z + 82 = 0$$